## Chapter 10 Review Sheet

## Use the following information for questions 1-3:

Do boys perform better in math than girls? A randomly selected group of each gender were given the same math assessment. The score results in the sample were:

|  | Boys | Girls |
| :---: | :---: | :---: |
| n | 110 | 135 |
| Mean | 71.6 | 68.3 |
| Standard Deviation | 10.4 | 11.2 |

1. What would be the null and alternative hypotheses of a test to determine if boys' scores were higher than girls' scores?
(a) $\mathrm{H}_{0}: \mu_{\mathrm{b}}-\mu_{\mathrm{g}}=0, \mathrm{H}_{\mathrm{a}}: \mu_{\mathrm{b}}-\mu_{\mathrm{g}}<0$
(b) $\mathrm{H}_{0}: \mu_{\mathrm{b}}-\mu_{\mathrm{g}}=0, \mathrm{H}_{\mathrm{a}}: \mu_{\mathrm{b}}-\mu_{\mathrm{g}} \neq 0$
(c) $\mathrm{H}_{0}: \mu_{\mathrm{b}}-\mu_{\mathrm{g}}=0, \mathrm{H}_{\mathrm{a}}: \mu_{\mathrm{b}}-\mu_{\mathrm{g}}>0$
(d) $\mathrm{H}_{0}: \mu_{\mathrm{b}}-\mu_{\mathrm{g}}<0, \mathrm{H}_{\mathrm{a}}: \mu_{\mathrm{b}}-\mu_{\mathrm{g}}=0$
(e) $\mathrm{H}_{0}: \mu_{\mathrm{b}}=\mu_{\mathrm{g}}, \mathrm{H}_{\mathrm{a}}: \mu_{\mathrm{b}} \neq \mu_{\mathrm{g}}$
2. What procedure would you use for this test?
3. Suppose the P-value of the test is .0344 . We can then conclude:
(a) At $\alpha=.025$, reject $\mathrm{H}_{0}$.
(b) At $\alpha=.02$, reject $\mathrm{H}_{0}$.
(c) At $\alpha=.01$, reject $\mathrm{H}_{0}$.
(d) At $\alpha=.025$, fail to reject $\mathrm{H}_{0}$.
(e) No conclusion can be drawn from this information.
4. There are two common methods for measuring the concentration of a pollutant in fish tissue. Do the two methods differ, on average? You apply both methods to each fish in a random sample of 18 carp and use:
(a) the paired $t$ test for $\mu_{d}$.
(b) the one-sample $z$ test for $p$.
(c) the two-sample $t$ test for $\mu_{1}-\mu_{2}$.
(d) the two-sample $z$ test for $p_{1}-p_{2}$.
(e) none of these.
5. Which of the following describes a Type II error in the context of this study?
(a) Finding convincing evidence that the true means are different for males and females, when in reality the true means are the same.
(b) Finding convincing evidence that the true means are different for males and females, when in reality the true means are different.
(c) Not finding convincing evidence that the true means are different for males and females, when in reality the true means are the same.
(d) Not finding convincing evidence that the true means are different for males and females, when in reality the true means are different.
(e) Not finding convincing evidence that the true means are different for males and females, when in reality there is convincing evidence that the true means are different.
6. A researcher reports that $80 \%$ of high school graduates, but only $40 \%$ of high school dropouts, would pass a basic literacy test. Assume that the researcher's claim is true. Suppose we give a basic literacy test to a random sample of 60 high school graduates and a separate random sample of 75 high school dropouts. Let $\hat{p}_{G}$ and $\hat{p}_{D}$ be the sample proportions of graduates and dropouts, respectively, who pass the test.
a) What is the shape of the sampling distribution of $\hat{p}_{G}-\hat{p}_{D}$ ?
b) Find the mean of the sampling distribution.
c) Find the standard deviation of the sampling distribution.
7. The heights of young men follow a Normal distribution with mean 69.3 inches and standard deviation 2.8 inches. The heights of young women follow a Normal distribution with mean 64.5 inches and standard deviation 2.5 inches. Suppose we select independent SRSs of 16 young men and 9 young women and calculate the sample mean heights $\bar{x}_{M}$ and $\bar{x}_{W}$.
a) What is the shape of the sampling distribution of $\bar{x}_{M}-\bar{x}_{W}$ ?
b) Find the mean of the sampling distribution.
c) Find the standard deviation of the sampling distribution.
8. A person released from prison before completing the original sentence is placed under the supervision of a parole board. If that person violates specified conditions of good behavior during the parole period, the board can order a return to prison. The article "Impulsive and Premeditated Homicide: An Analysis of the Subsequent Parole Risk of the Murderer" reported the data on parole behavior below. One random sample of individuals had served time in prison for impulsive murder, and the other random sample had served time for premeditated murder. Construct and interpret a $98 \%$ confidence interval for the difference in the proportions of individuals serving time for impulsive murder and individuals serving time for premeditated murder who successfully completed parole.

|  | Impulsive | Premeditated |
| :--- | :---: | :---: |
| Sample size | 42 | 40 |
| Number with no violation | 13 | 22 |
| Sample proportion | .310 | .550 |

9. A study of iron deficiency in infants compared independent random samples of infants whose mothers chose different ways of feeding them. One group contained breast-fed infants. The children in another group were fed a standard baby formula without any iron supplements. Here are summary results on blood hemoglobin levels at 12 months of age. Graphical displays of the sample data show no strong skewness and no outliers.

| Group | n | $\bar{x}$ | s |
| :--- | :--- | :--- | :--- |
| Breast-Fed | 23 | 13.3 | 1.7 |
| Formula | 19 | 12.4 | 1.8 |

Is there significant evidence at the $\alpha=0.05$ level that the mean hemoglobin level is different among breast-fed babies?
10. Patients with heart-attack symptoms arrive at an emergency room either by ambulance or selftransportation provided by themselves, family of friends. When a patient arrives at the emergency room, the time of arrival is recorded. The time when the patient's diagnostic treatment begins is also recorded. An administrator of a large hospital wanted to determine whether the mean wait time (time between arrival and diagnostic treatment) for patients with heart-attack symptoms differs according to the mode of transportation. Independent random samples of 75 patients with heart-attack symptoms who had reported to the emergency room via each mode of transportation were selected. For each patient, the wait time was recorded. Summary statistics for each mode of transportation are shown in the table below.

| Mode of <br> Transportation | Sample Size | Mean Wait Time (in <br> minutes) | Standard Deviation of <br> Wait Times (in <br> minutes) |
| :--- | :--- | :--- | :--- |
| Ambulance | 75 | 6.04 | 4.30 |
| Self | 75 | 8.30 | 5.16 |

a) Construct and interpret a $99 \%$ confidence interval to estimate the difference between the mean wait times for ambulance-transported patients and self-transported patients at this emergency room.
b) Based only on this confidence interval, is there a significant difference in mean wait times? Justify your answer.

## Chapter 10 Learning Targets:

_ I can describe the sampling distribution of $\hat{p}_{1}-\hat{p}_{2}$.
_ I can construct and interpret a two-proportion z interval.
_ I can carry out a two-proportion z test.
_ I can explain the reason for using $\hat{p}_{C}$ in a two-proportion z test.
_ I can describe the sampling distribution of $\bar{x}_{1}-\bar{x}_{2}$.
_ I can construct and interpret a two-sample z interval.
_ I can construct and interpret a two-sample $t$ interval.
_ I can find the degrees of freedom for using t procedures using a conservative estimate or a calculator.
_ I can carry out a two-sample z test.
_ I can carry out a two-sample t test.

